## REPORT No. 379

# ROLLING MOMENTS DUE TO ROLLING AND YAW FOR FOUR WING MODELS IN ROTATION

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### SUMMARY

This report presents the results of a series of autorotation and torque tests on four different rotating wing systems at various rates of roll and at several angles of yaw. The investigation covered an angle-of-attack range up to 90° and angles of yaw of 0°, 5°, 10°, and 20°. The tests were made in the 5-foot, closed-throat atmospheric wind tunnel of the National Advisory Committee for Aeronautics. The object of the tests was primarily to determine the effects of various angles of yaw on the rolling moments of the rotating wings up to large angles of attack.

It was found that at angles of attack above that of maximum lift the rolling moments on the wings due to yaw (or side slip) from  $5^{\circ}$  to  $20^{\circ}$  were roughly of the same magnitude as those due to rolling. There was a wide variation in magnitude of the rolling moment due to yaw angle with both angle of attack and with  $\frac{pb}{2V}$ . The rates and ranges of stable autorotation for the monoplane models were considerably increased by yaw, whereas for an unstaggered biplane they were little affected. The immediate cause of the rolling moment due to yaw is apparently the building up of large loads on the forward wing tip and the reduction of loads on the rearward wing tip.

#### INTRODUCTION

The rotational motion which is characteristic of the spin of an airplane is due chiefly to certain rolling moments produced by the wings. These moments arise as the result of three principal causes:

- 1. The rotational motion itself.
- 2. The angle of yaw or side slip.
- 3. The ailerons.

The rolling moment due to the angular velocity in roll has until recently been thought of as the primary cause of the spin. It has been the subject of a number of wind-tunnel and mathematical investigations such as the one given in Reference 1. The mathematical analyses have been based upon the "strip method" of determining the rolling moments due to rolling for various wing systems.

Certain investigations have indicated that an additional large rolling moment is produced at angles

of attack beyond that of maximum lift when a wing is given an angular displacement in yaw. That this moment exists when the wing is stationary is shown in References 2, 3, 4, and 5, and some of the anomalous effects produced by it in the case of certain airplanes in stalled flight are indicated in References 6 and 7. Chief of the effects due to yaw and to yawing (References 6 and 7) is the apparent reversal of aileron control, since at large angles of attack the instrumental records show that the ultimate roll is in a direction opposite to that which the ailerons would normally produce. The rolling moment due to yaw also persists when the wing is rotating, as is shown in References 8 and 9, which describe wind-tunnel investigations wherein the models were free to rotate about a central axis parallel to the wind direction. This fact is indicated by the increased rates and angular ranges of stable autorotation which obtained when the models were given an angle of yaw.

The present report does not include a study of the variation in alleron characteristics with yaw and rate of roll, since it was necessary to limit the variables in order to complete the tests within a reasonable length of time. This phase of the subject is partially covered in References 10 and 11.

So far as the writers have been able to ascertain, no tests had previously been made in which rolling moments were measured on a rotating wing at various angles of yaw. The object of this wind-tunnel investigation, which was conducted at the Langley Memorial Aeronautical Laboratory, was to supply such information. A partial explanation is given of the relatively large rolling moments due to yaw occurring at large angles of attack.

The tests were made in the 5-foot atmospheric wind tunnel (Reference 12) on models of four representative wing systems: namely, an unstaggered biplane and three different monoplane wings. The rolling moments were measured on a small electric dynamometer designed especially for the purpose. A large range of angles of attack was covered.

### MODELS AND APPARATUS

The models used consisted of one biplane and three different monoplane wings. The biplane had zero

stagger and a gap/chord ratio of 1.0. Both upper and lower wings had a 5-inch chord and were of aspect ratio 6. The tips were circular and the Clark Y profile was used. Figure 1 shows the general arrangement of this model. One wing of the biplane was also tested as a monoplane wing, and is shown as such in Figure 2.

The second monoplane-wing model had the N. A. C. A. 84 profile, but was rectangular in plan form except for the tips. These were faired, as shown in the diagram of the wing, Figure 3. The model also had a 5-inch chord and an aspect ratio of 6.

The third monoplane-wing model was designated as the N. A. C. A. 86-M and was tapered in plan

An arm attached to the cradle at right angles to the knife edges transmits the torques to a balance outside of the tunnel (fig. 6), upon which the rolling moments for rotations in either direction are measured. The dynamometer assembly is housed in an aluminum fairing, as shown in Figure 7, which is a view of the installation in the 5-foot closed-throat atmospheric wind tunnel.

The wing was mounted on the dynamometer-shaft extension arm, as shown. A simple clamp arrangement on the model, and the angle-of-attack changing mechanism outside the tunnel (fig. 8) permitted the angle of attack to be varied as desired. The rate and direction of rotation were controlled by a variable-speed

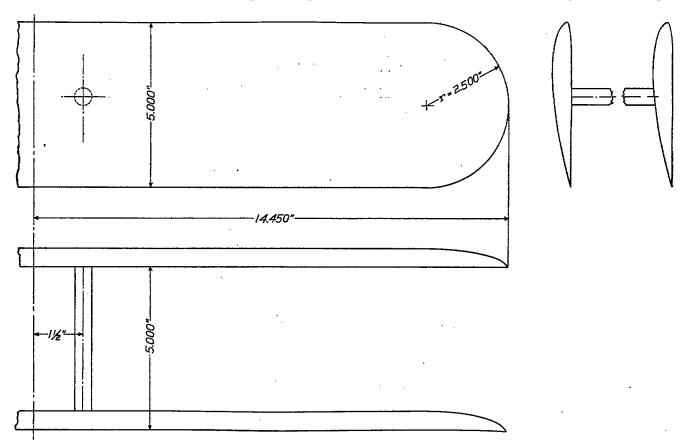


Figure 1.—Biplane wing model—Clark Y

and thickness, having a ratio of tip chord to root chord of 0.5. The N. A. C. A. 84 profile was used at the root section and the N. A. C. A.—M2 profile at the tips, which were circular in plan. The model had an aspect ratio of 6, and is shown in Figure 4.—

All of the models were made of laminated mahogany. In the construction of the models the profile ordinates were held accurate to within  $\pm 0.003$  inch of those listed in Tables I, II, and III.

The autorotation dynamometer consists essentially of a shaft parallel to the air stream and rotating on ball bearings. It is driven through reduction gearing by a small, direct-current motor mounted in a cradle on knife-edges. (See fig. 5.)

motor with a reversing switch, used in conjunction with a stroboscopic tachometer and stop watch. The angle of yaw was adjusted by clamping the model at the desired position on its supporting arm, using an inclinometer placed on the leading edge to indicate the angle.

#### TESTS

Before making the actual autorotation tests on the various models a few preliminary tests were made for calibration purposes. With the dynamometer in place, but without any model mounted on the extension arm, vertical velocity surveys were made at approximately the location of the model. A Pitot-static tube, installed permanently in the tunnel sufficiently far upstream from the model to be unaffected by it, was then cali-

brated against the integrated mean of the final survey and used as a dynamic pressure reference.

Tare rolling-moment tests were then made to determine the magnitude of the effects due to the ball-bear-

foot, corresponding to an average air speed of 39.8 m. p. h. For comparison with pressure-distribution tests the dynamic pressure was maintained at 5.01 pounds per square foot for the tests on the N. A. C. A.

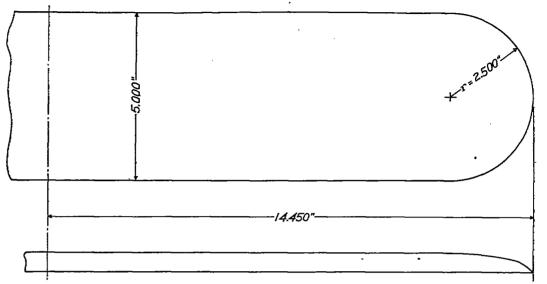


FIGURE 2.—Monoplane wing model—Clark Y

ing friction and windage of the model support arm. With the tunnel operating, the arm was driven by the dynamometer motor at speeds ranging from 0 to 500 r. p. m., and the rolling moments were measured at several points for rotations in both positive and negative directions. Curves were then plotted, and from

84 wing model, since a slight scale effect was found to exist at the two different pressures.

When making the stable autorotation tests, the model was allowed to rotate freely by merely disengaging the reduction gearing in the dynamometer. The rates of rotation in both directions at various angles of

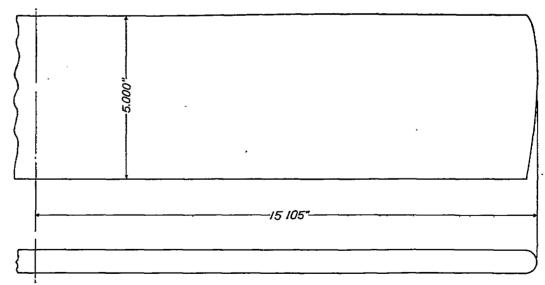


FIGURE 3.—Monoplane wing model—N. A. C. A. 84

these the total rolling moments due to the models were corrected.

The tests on each wing model were made in two parts:

- 1. Stable autorotation tests.
- 2. Rolling moment tests.

In general the angle-of-attack range was from 0° to 90°, and angles of yaw were set at 0°, 5°, 10°, and 20°. Rotations of the models were varied between 0 and 500 r. p. m. and were taken in both positive and negative directions. The tests were made on three of the models at a dynamic pressure of 4.05 pounds per square

attack were measured by counting the revolutions for a period of time. In addition the angles of attack between which the model would start rotating of itself, and also those at which it did not quite rotate when given a start by hand, were observed.

The rolling-moment tests were made with the dynamometer gearing in mesh, so that the speed of rotation was controlled by the motor. Static moments were first measured with the tunnel operating, and then not operating, for the model both in the normal position of flight and then inverted. Moments due to

the rotation were obtained for both directions at various rates and angles of attack. Rotation of the model was measured by counting the revolutions for a period of time for low rates of rotation and by use of the stroboscopic tachometer for the higher rates.

As the result of check tests, the probable accuracy obtained in the investigation was estimated as follows:

- (a) Angle-of-attack setting— $\pm 0.2^{\circ}$ .
- (b) Angle-of-yaw setting— $\pm 0.2^{\circ}$ .
- (c) Rolling-moment balance—±0.5 gram.
- (d) R. p. m. measurements— $\pm 1.0$  per cent.
- (e) Dynamic pressure ± 0.75 per cent.
- (f) Data as tabulated— $\pm 3.0$  per cent.

of the wing in the plane of rotation to the wind velocity. This coefficient, which is nondimensional, may be defined as follows:

$$\frac{pb}{2V}$$
 = tan  $\varphi_t$ 

where

p =angular velocity (radians per second).

b = span of wing.

 $\overline{V}$  = wind velocity.

 $\varphi_i$  = difference between angle of attack at the wing tip and that at mid span.

The rolling-moment coefficient,  $C_{\lambda}$ , was used as applying to a wing when in rotation, rather than the

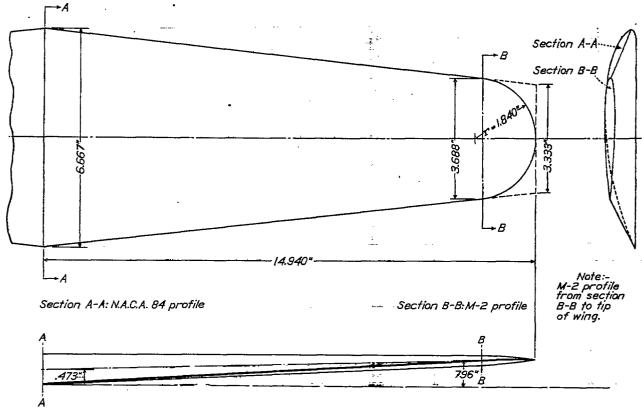


FIGURE 4.-Monoplane wing model-N. A. C. A. 86-M

The rates of stable autorotation were not corrected for the friction of the ball bearings, but this error is probably not greater than -2 per cent.

### RESULTS

The results are presented as absolute coefficients in both tabular and graphical form. Tables IV to VII, inclusive, list the results of the stable-autorotation tests for the four wing models at various angles of attack and yaw, and Tables VIII to XXI give the results of the rolling-moment tests. Figures 9 to 35 give the results in the form of curves.

 $rac{pb}{2V}$  actually represents the ratio of the linear tip speed

usual rolling-moment coefficient which is ordinarily used for a nonrotating wing. It should be noted, however, that  $C_{\lambda}$  is identical with  $C_{z}$  at zero rate of rotation. The former may be defined as:

$$C_{\lambda} = \frac{\lambda}{abS}$$

where

 $C_{\lambda}$  = absolute coefficient of rolling moment,

λ = measured rolling moment about dynamometer axis,

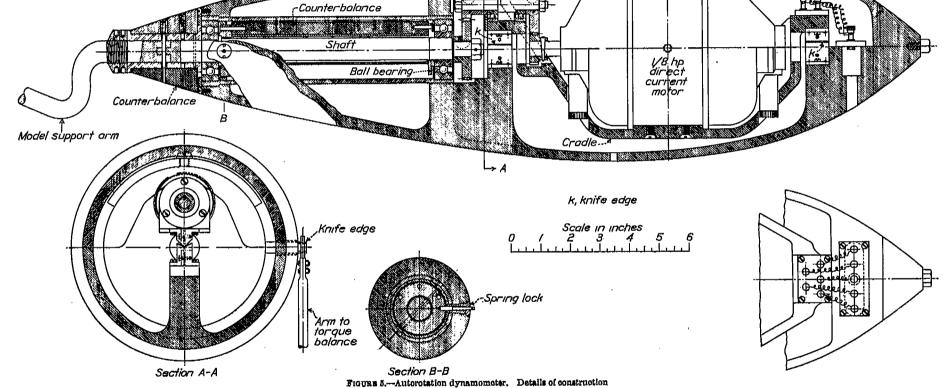
S =area of the wing.

b =span of the wing,

q =dynamic pressure,

all in a consistent system of units.

Cover



Reduction gearing

#### DISCUSSION

A general analysis of the rolling moments due to rolling and yaw will first be made, using as a basis the N. A. C. A. 84 monoplane wing, for which not only autorotation but also pressure-distribution data are available. A comparison will then be made of the autorotation test results on all four wing models.

the angle-of-attack axis was always normal to the wind direction in these tests. (See Table XXVII for standard equivalents.)

The characteristic curves of rolling-moment coefficient,  $C_{\lambda}$ , due to rolling (yaw=0°) versus  $\frac{pb}{2V}$  for the N. A. C. A. 84 wing, as obtained on the dyna-



FIGURE 6.-Torque balance installation

In the tests the axis of yaw was in a plane parallel to the wind direction and normal to the plane of the wing chords. This is not the conventional axis of yaw. However, the design of the dynamometer apparatus as used in these tests permitted yawing the wing only about this axis. It is also to be noted that

mometer, are shown in Figure 9. The dashed portions of the curves represent estimated fairings where it was impossible to obtain test data, owing to instability of the wing and dynamometer combination. Small moments occurring at  $\frac{pb}{2V}$ =0 are due to asym-

metry of the models or of the air flow in the tunnel. Rolling moments for rotations in both directions are plotted. Clockwise is positive and counter clockwise is negative direction of rotation.

The significance of these curves will be described briefly. Moments plotted in the first and third quadrants are those which aid, and in the second and fourth those which oppose, rotation. The change in the shape of the curves between  $\alpha=12^{\circ}$  and  $\alpha=18^{\circ}$ 

and the wing would come to rest. If, on the other hand, the disturbance increased the angular velocity, a moment aiding the rotation would be built up, reaching a maximum at about  $\frac{pb}{2V}$ =0.26, and then decreasing to zero at  $\frac{pb}{2V}$ =0.35. Here the rolling moment is once more zero, and since the slope of the curve is now negative, or opposite to the slope at the

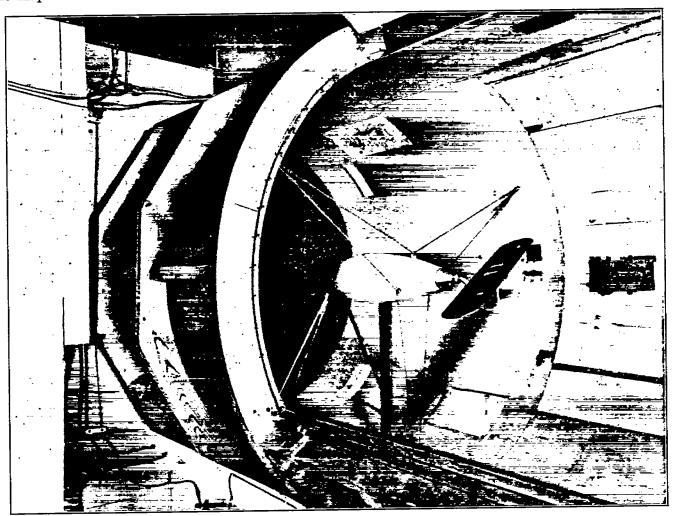


FIGURE 7.—Wing and dynamometer set-up in wind tunnel

is noteworthy and characteristic of angles in the vicinity of maximum lift.

Let us now consider the curve for  $\alpha=16^{\circ}$ . If the wing is started rotating in the positive direction, a moment opposing the rotation is set up. This moment reaches a maximum at  $\frac{pb}{2V}=0.12$ , thereupon decreasing until it becomes zero at  $\frac{pb}{2V}=0.19$ . At this point the wing would rotate of its own accord if it were not for the unstable condition represented by the positive slope of the curve as it crosses the axis. In other words, if the wing were left to itself at this point, a small disturbance tending to reduce the angular ve-

locity would result in setting up a retarding moment,

first intersection with the axis, a stable condition results, so that the wing will now rotate continuously, regardless of small momentary disturbances. The first condition may be termed "unstable autorotation" and the second "stable autorotation."

It is evident that if the model were mounted so as to rotate freely when disturbed from rest, its rotation would build up until the stable-autorotation point for the particular angle of attack was reached. (This point will be attained, however, only if the disturbance is of sufficient magnitude to carry the rotation beyond any unstable-autorotation points first encountered.) The results of such a stable-autorotation test on the N. A. C. A. 84 wing are given in Figure 10, in which

 $\frac{p\,b}{2\,V}$  is plotted versus angle of attack,  $\alpha$ . To obtain the data for this curve, the dynamometer gearing was thrown out of mesh so that the model could turn freely with the shaft, which is mounted on ball bearings, as explained previously. The reversal of the direction of the curve near  $\alpha=15^\circ$  can be explained by reference again to the curve for  $\alpha=16^\circ$  in Figure 9. Here it will be seen that the model must be forced to rotate up to the point of unstable autorotation, beyond which it will rotate of its own accord. This point, together

Figure 11, which has the same ordinates as the figure for zero yaw (Fig. 9). The convention adopted in this figure is that for positive values of  $\frac{pb}{2V}$  the rolling moments due to the yaw and the roll are in the same sense, and for negative values they oppose each other. For the tests in yaw the wing was given only positive yaw, i. e., the right wing tip was back, but rotations were taken in both positive and negative directions.

The general effect of yaw is to raise the curves as a group. It will also be seen that large moments now

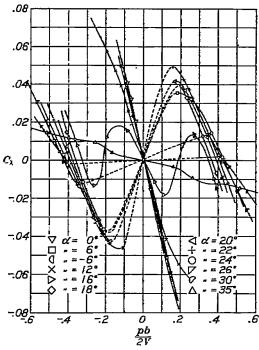


FIGURE 8.-Mechanism inserted for changing angle of attack

with the stable-autorotation points, as obtained from the moment curves of Figure 9, is plotted in Figure 10. The slight differences between these points and the curve are due to the small tare moments produced by friction in the ball bearings and the windage of the arm supporting the model. The point on the axis at  $\alpha=21^{\circ}$  was obtained by decreasing the angle until the wing would no longer rotate when disturbed slightly from rest.

Let us now consider the rolling moment due to yaw. The total rolling moments due to both rolling and yaw for the N. A. C. A. 84 wing (yaw=10°) are plotted in

exist at  $\frac{pb}{2V} = 0$ . The changes in rolling moment due to yaw with changes in  $\frac{pb}{2V}$  are of interest, and these are shown in Figure 12 for five selected angles of attack. These curves were obtained merely by taking the differences between the corresponding curves of rolling moment due to rolling (fig. 9) and rolling moment due to rolling and yaw (fig. 11). They indicate that the maximum moments due to yaw occur at the angles of attack of stable autorotation and in the vicinity of  $\frac{pb}{2V} = 0$ . The variation with  $\frac{pb}{2V}$  is much greater



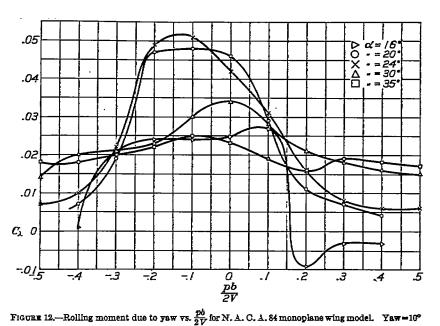


Figure 9.—Rolling moment coefficient vs.  $\frac{pb}{2V}$  for N. A. C. A. 84 monoplane wing model. Yaw=0°

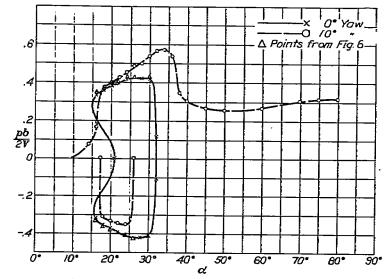
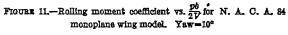
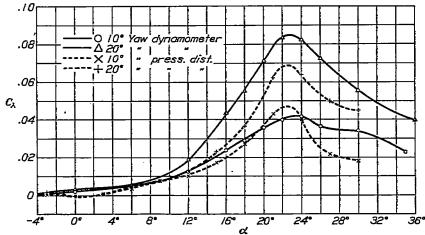


FIGURE 10.— $\frac{pb}{2V}$ vs. angle of attack for N. A. C. A. 84 monoplane wing model. Yaw=0°, 10°







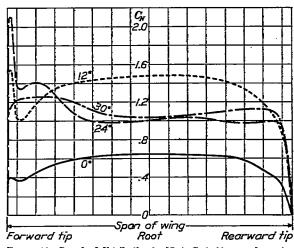


FIGURE 14.—Span load distribution for N. A. C. A. 84 monoplane wing model. Yaw=10°

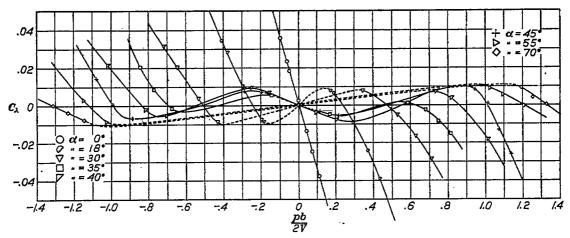


Figure 15.—Rolling moment coefficient vs.  $\frac{pb}{2V}$  for Clark Y biplane wing model. Yaw=0°

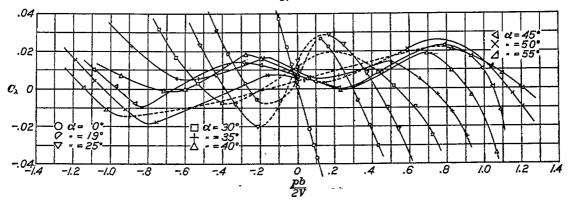


Figure 16.—Rolling moment coefficient vs.  $\frac{pb}{2V}$  for Clark Y biplane wing model. Yaw=5°

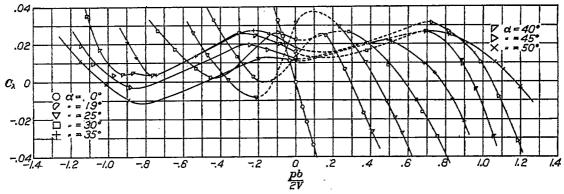


Figure 17.—Rolling moment coefficient vs.  $\frac{pb}{2V}$  for Clark Y biplane wing model. Yaw=10°

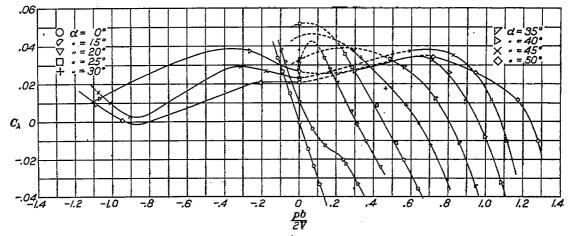


Figure 18.—Rolling moment coefficient vs.  $\frac{pb}{2V}$  for Clark Y biplane wing model. Yaw=20°

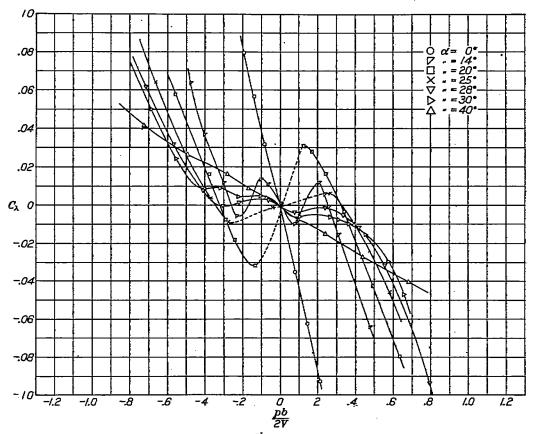


Figure 19.—Rolling moment coefficient vs.  $\frac{pb}{2V}$  for Clark Y monoplane wing model. Yaw=0°

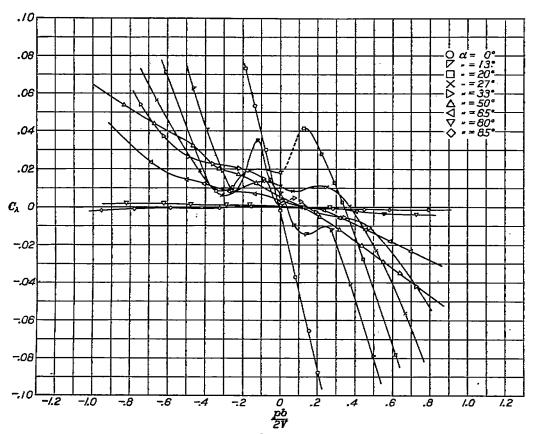


Figure 20.—Rolling moment coefficient vs.  $\frac{pb}{2V}$  for Clark Y monoplane wing model. Yaw=5°

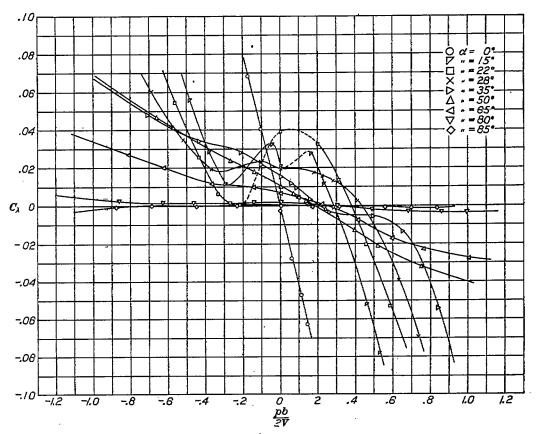


Figure 21.—Rolling moment coefficient vs.  $\frac{pb}{2V}$  for Clark Y monoplane wing model. Yaw=10°

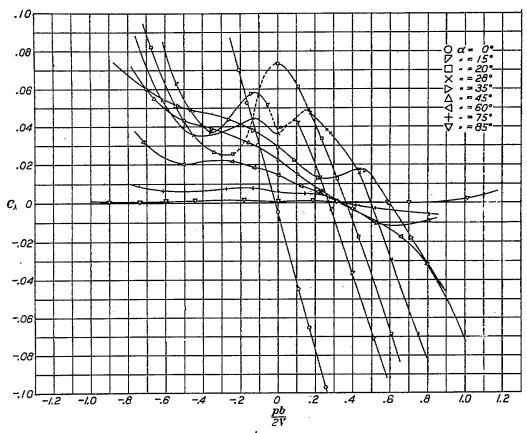


Figure 22.—Rolling moment coefficient vs.  $\frac{p}{2V}$  for Clark Y monoplane wing model. Yaw=20°

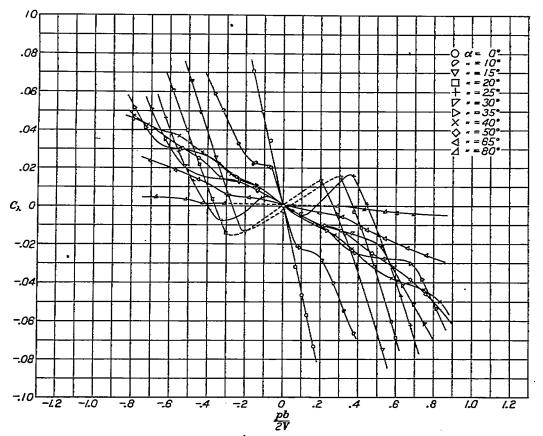


Figure 23.—Rolling moment coefficient vs.  $\frac{pb}{2V}$  for N. A. C. A. 85–M monoplane wing model. Yaw=0°

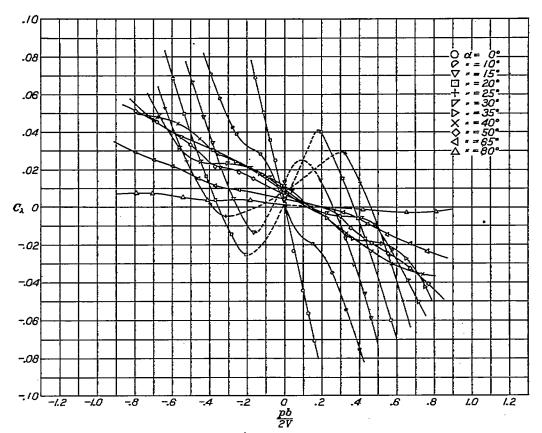


Figure 24.—Rolling moment coefficient vs.  $\frac{pb}{2V}$  for N. A. C. A. 86-M monoplane wing model. Yaw=5°

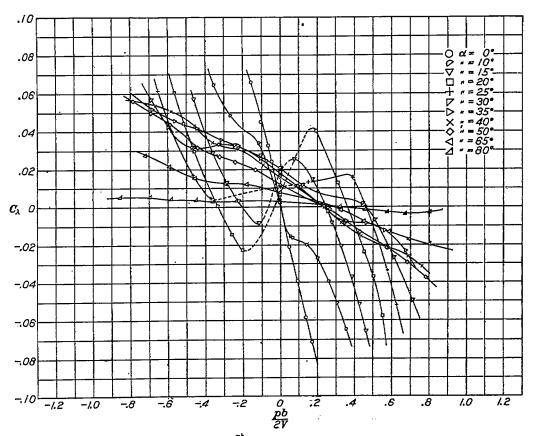


Figure 25.—Rolling moment coefficient vs.  $\frac{pb}{2V}$  for N. A. O. A. 86-M monoplane wing model. Yaw=10°

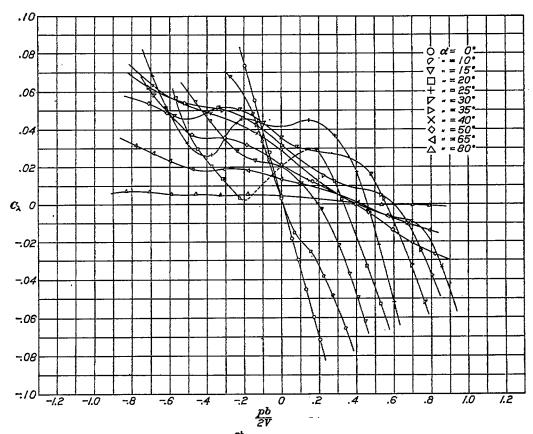


Figure 26.—Rolling moment coefficient vs.  $\frac{pb}{2V}$  for N. A. C. A. 86-M monoplane wing model. Yaw=20°

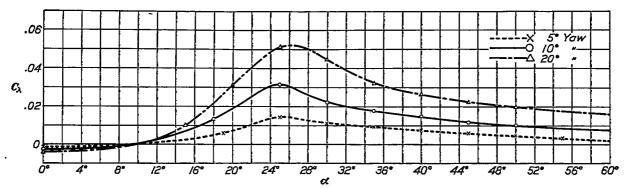


Figure 27.—Rolling moment due to yew vs. angle of attack for Clark Y biplane wing model. Yaw=5°, 10°, 20°.  $\frac{pb}{2V}$ =0

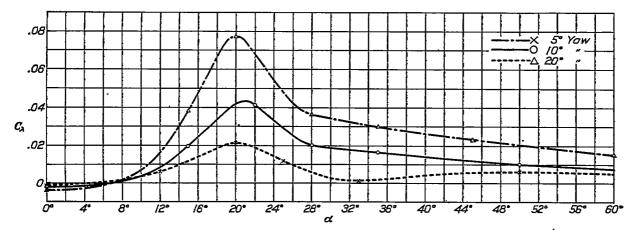


Figure 28.—Rolling moment due to yew vs. angle of attack for Clark Y monoplane wing model. Yaw=5°, 10°, 20°.  $\frac{pb}{2V}$ =0

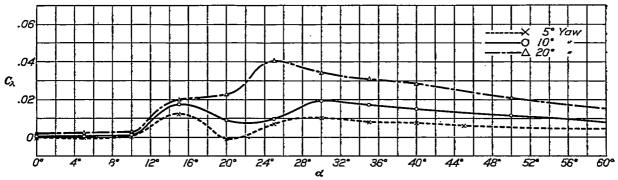


Figure 29.—Rolling moment due to yaw vs. angle of attack for N. A. C. A. 86-M monoplane. Yaw=5°, 10°, 20°.  $\frac{pb}{2V}$ =0

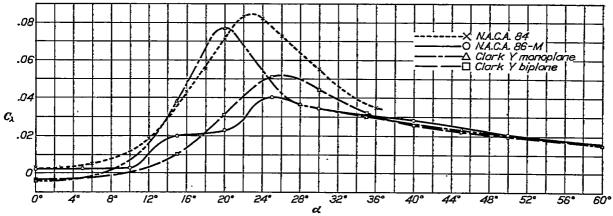


FIGURE 30.—Rolling moment due to yaw vs. angle of attack for four wing models. Yaw=20°.  $\frac{P^b}{2V}$ =0

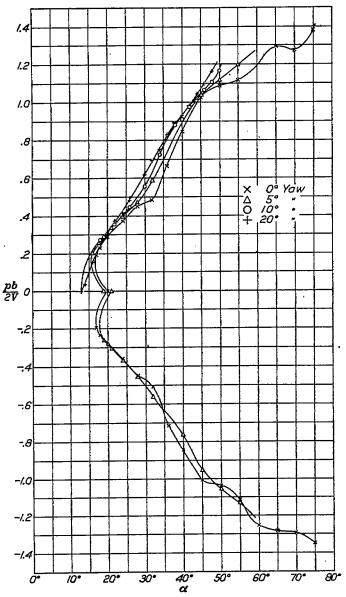


Figure 31.  $-\frac{pb}{2V}$  vs. angle of attack for Clark Y biplane wing model. Yaw=0°, 5°, 10°, 20°

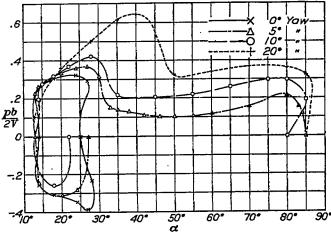


Figure 32.  $-\frac{p\delta}{2V}$  vs. angle of attack for Clark Y monoplane wing model. Yaw=0° 5°, 10°, 20°

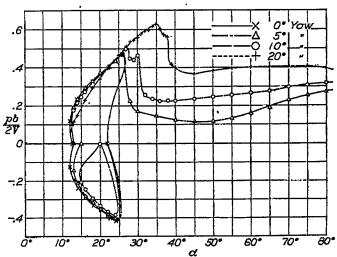


FIGURE 38.  $-\frac{pb}{2V}$  vs. angle of attack for N. A. C. A. 35-M monoplane wing model. Yaw=0°, 5°, 10°, 20°

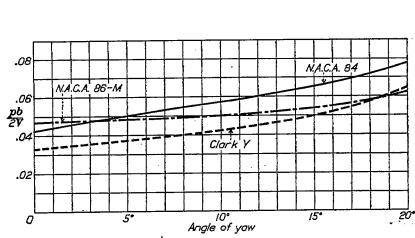


Figure 35.—Maximum  $\frac{pb}{2V}$  vs. angle of yaw for three monoplane wing models

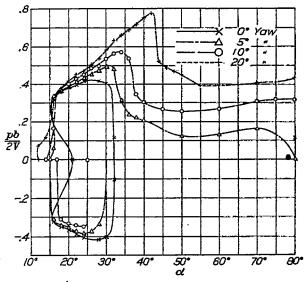


FIGURE 34.  $-\frac{\mathcal{D}b}{2\mathcal{V}}$  vs. angle of attack for N. A. O. A. 84 monoplane wing model. Yaw=0°, 5°, 10°, 20°

between  $\alpha=16^{\circ}$  and  $\alpha=30^{\circ}$  than above the latter angle. It is of importance to note that positive moments for positive values of  $\frac{pb}{2V}$  aid rotation, while

positive moments for negative values of  $\frac{pb}{2V}$  oppose it.

The curves of stable autorotation for 10° yaw for rotations in both directions are included in Figure 10. The marked differences in values of  $\frac{pb}{2V}$  and in ranges agree with similar tests of this type described in References 7 and 8, mentioned previously. For positive values of  $\frac{pb}{2V}$ , rate and range of autorotation is consider-

ably increased, while for negative values it is reduced. A knowledge of the manner in which the span load distribution changes to produce a rolling moment when a wing is yawed may be expected to be of value in determining the reason for the existence of this peculiar moment at large angles of attack. A limited amount of such information is available for the N. A. C. A. 84 monoplane wing as the result of recent pressure-distribution tests. In certain of these tests the half-span wing model used was given an angle of sweep back and also sweep forward. The pressure-distribution results were analyzed on the basis of yaw by considering that yaw is equivalent to sweep forward on one half of the span and sweep back on the other half. The full-span rolling moments due to 10° and 20° yaw obtained in this manner from the half-span wing results are plotted in Figure 13, together with the moments obtained on the full-span wing mounted on the dynamometer. While the agreement is only fair, the trend is the same in each case and furnishes a justification for using the sweep-back and sweep-forward results for the purpose of this analysis.

The span-load distribution, as thus determined, is plotted in Figure 11 for a few selected angles. The cause of the rolling moment is at once apparent, for it is evident that as the angle of attack increases the loads increase on the forward wing, particularly at the tip, while the reverse is true for the rearward wing. This has also been found to be the case as a result of pressure-distribution tests made on a full-span wing model at various angles of yaw. (Reference 5.)

Let us now turn to a consideration of the results of tests on the other three wing systems: namely, the Clark Y unstaggered biplane, the Clark Y monoplane, and the N. A. C. A. 86-M monoplane. The characteristic curves of rolling-moment coefficient,  $C_{\lambda}$ , versus  $\frac{pb}{2V}$  are given for yaw =0°, 5°, 10°, and 20° in Figures 15 to 26.

The values of  $C_{\lambda}$  at  $\frac{pb}{2V}$ =0 are plotted versus  $\alpha$  for each wing at 5°, 10°, and 20° yaw in Figures 27, 28, and 29. The curves of this type for all four wing

models at 20° yaw are assembled for comparison in Figure 30. It should be remembered, however, that the effect of the different-shaped tips is also included in this comparison, although the effects may be small. The maxima for all four curves occur between  $\alpha = 20^{\circ}$ and 26°. The negative moments for the Clark Y models are probably due to the negative dihedral effect of the tips. (See figs. 1 and 2.) The Clark Y and N. A. C. A. 84 monoplane wings show similar results up to the vicinity of their maxima, beyond which the moments for the N. A. C. A. 84 wing are greater. The Clark Y biplane wing moments are much less than those for the Clark Y monoplane wing between  $\alpha = 6^{\circ}$ and  $\alpha=25^{\circ}$ , and greater beyond this angle up to  $\alpha = 36^{\circ}$ , above which they are almost identical for the limits of the tests. In fact, it appears that the values for all the wings may be expected to be practically the same above  $\alpha=36^{\circ}$ . The value of the maximum moments decreases in the following order: N. A. C. A. 84 monoplane, Clark Y monoplane, Clark Y biplane, and N. A. C. A. 86-M monoplane. The peculiar additional bend in the N. A. C. A. 86-M curve at about  $\alpha = 14^{\circ}$  should be noted.

The stable-autorotation characteristics of each wing at 0°, 5°, 10°, and 20° yaw are given in Figures 31 to 34. All of the monoplane-wing results are affected in the same general manner when the angle of yaw is increased, there being a general increase in both the rates and ranges of autorotation. The variation of the maximum values of  $\frac{pb}{2V}$  with angle of yaw are plotted for the three monoplane wings in Figure 35. A yaw of 20° practically doubles the maximum value of  $\frac{pb}{2V}$  at zero yaw for the N. A. C. A. 84 and Clark Y monoplanes, whereas for the N. A. C. A. 86-M wing the increase is only about one-third. The biplane stable-autorotation rates are not greatly changed by yaw, as may be seen in Figure 31.

In order that a wing have dynamic lateral stability, it is essential, among other things, that a righting (rolling) moment due to side slip (yaw) be accompanied by a damping moment due to roll. Below the stall the damping moments are usually ample for stability in comparison with the righting moments. In general above the stall, however, the damping moment changes sign and becomes an accelerating moment, and the righting moment due to side slip assumes large proportions. A possibility of improving this situation would be to seek for some means of reducing the rolling moments due to rolling and yaw. A study of the curves in Figures 9, 15, 19, and 23 indicates that the maximum rolling moments due to rolling can be reduced a considerable extent by using an unstaggered biplane wing or by tapering a monoplane wing in plan and thickness.

Several additional subjects for future investigation suggest themselves as a result of this work. One of importance is the further study of biplane wings to determine the effects of stagger and gap on the rolling moments due to rolling and to yaw. In the same connection an investigation of more highly tapered wings than are now in use would also appear to furnish some useful information regarding the monoplane characteristics.

#### CONCLUSIONS

- 1. At angles of attack above that of maximum lift the rolling moments on wings due to yaw (or side slip) from 5° to 20° are of the same order of magnitude as those due to rolling.
- 2. There is a wide variation in the magnitude of the rolling moment due to yaw angle with both angle of attack and rate of roll.
- 3. The rates and ranges of stable autorotation for the monoplane wings are considerably increased by yaw, whereas for an unstaggered biplane they are little affected.
- 4.—The immediate cause of the rolling moment due to yaw angle is, apparently, the building up of large tip loads on the forward wing and the reduction of tip loads on the rearward wing.

LANGLEY MEMORIAL AERONAUTICAL LABORATORY,
NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS,
LANGLEY FIELD, VA., August 19, 1930.

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TABLE I.—ORDINATES, CLARK Y WING
[Monoplane and biplane]

Station (% c from L. E.)	Upper (%c)	Lower (% c)	Station (% c from L. E.)	Upper (%c)	Lower (% c)
0 1. 25 2. 50 5. 60 7. 50 10. 00 15. 00 20. 00 30. 00	3. 50 5. 45 6. 50 7. 90 8. 85 9. 60 10. 69 11. 30 11. 70	8.50 1.93 1.47 .93 .63 .42 .15	40.00 50.00 60.00 65.00 70.00 80.60 90.00 95.00	11. 40 10. 52 9. 15 8. 30 7. 35 5. 22 2. 82 1. 49 . 12	000000000

TABLE II.—ORDINATES, N. A. C. A. 84 WING

 Station (% c from L. E.)	Upper (% c)	Lower (% c)	Station (% c from L. E.)	Upper (% c)	Lower (% c)
-0 1. 25 2. 50 5. 50 7. 50 10. 00 15. 00 20. 00 25. 00	2.50 3.90 4.85 6.05 7.78 9.03 10.00 11.50 12.71 13.51	2.50 1.55 .95 .41 .10 .02 0	30, 00 35, 00 44, 00 50, 00 72, 00 86, 00 96, 00	14.00 14.18 14.11 13.50 12.31 10.32 7.71 4.39 2.41	00000000000

TABLE III.—ORDINATES, N. A. C. A. 86-M WING

Ro	Root section		Tip section		Root section			Tip section	
Station (% c from L. E.)	(% c Upper Lower from (% c) (% c)			Lower (%c)	Station (% c from L. E.)	Upper (% c)	Lower (% c)	Upper (% ¢)	Lower (% c)
0 1. 25 2. 50 8. 00 7. 50 10. 00 10. 00 20. 00 25. 00	2. 50 4. 85 6. 05 7. 78 9. 03 10. 00 11. 50 12. 71 13. 51	2.50 .95 .41 .10 .02 0	0 1. 30 1. 74 2. 83 2. 74 8. 05 8. 49 3. 78	0 -1.30 -1.74 -2.83 -3.74 -3.05 -3.49 -3.78	30. 00 40. 00 50. 00 60. 00 70. 00 90. 00 95. 00 100. 00	14.00 14.11 13.50 12.81 10.32 7.71 4.39 2.41 .30	00000	4.03 4.00 8.74 8.30 2.71 1.99 1.15 .69	-4. 03 -4. 00 -3. 74 -8. 30 -2. 71 -1. 99 -1. 15 69 20

TABLE IV.—STABLE-AUTOROTATION TESTS, BIPLANE WING, CLARK Y

i	Yaw=(	<b>)</b> °	Yaw=5°			ĺ	Yaw=10°			Yaw=20°		
a.	Positive rotation	Nega- tive rota- tion 20	α°	Positive rotation po	Nega- tive rota- tion pb 2V	α°	Positive rotation pb	Nega- tive rota- tion pb 2V	α°	Positive rotation pb 2V	Nega- tive rota- tion pb 2V	
17 18 20 24 28 32 36 40 45 55 60 65 70	0. 196 233 1. 291 1. 371 1. 453 .664 .842 1. 025 1. 083 1. 111 1. 192 1. 1, 296 1. 272 [ 1. 380 1. 027	0. 197 - 235 1. 278 1. 380 1. 448 - 508 - 718 - 846 1. 1034 1. 1034 1. 1264 1. 1264 1. 1263 1. 292 }1. 350	16 19 20 21 24 28 32 36 40 45 50	0.202 1.291 1.310 1.336 1.392 1.472 1.584 1.573 (1.202 1.040 11.034 11.111 11.1188	0 -261 -278 1 306 1 386 -452 -562 0 -762 -955 1 055 1 131	13 18 22 26 30 34 40 42 44 46 48 50		00 2867 2867 000000000	14 16 18 20 22 24 26 30 32 34 35 36 40 42 44 48	1 0. 034 1 154 1 250 1 380 1 373 1 416 1 483 1 584 1 694 1 754 1 830 1 830 1 929 1 980 1 1. 043 1 1. 064 1 1. 163	000000000000000000000000000000000000000	

<sup>&</sup>lt;sup>1</sup> Self-starting.

TABLE V.—STABLE-AUTOROTATION TESTS, MONOPLANE WING, CLARK  $\Upsilon$ 

7	Yaw=0°			Yaw=5°			Yaw=10°			Yaw=20°		
a*	Posi- tive ro- tation pb 2V	Nega- tive ro- tation <u>po</u> 2V	α°	Posi- tive ro- tation <u>pb</u> <b>2</b> V	Nega- tive ro- tation <u>pb</u> 2V	α°	Posi- tive ro- tation pb 2V	Nega- tive ro- tation po 2V	a•	Posi- tive ro- tation pb 2V	Neg- ative rota- tion pb 2V	
13.8 14.0 14.0 24.0 27.0 28.0 28.6	0 1, 257 1, 306 1, 323 291 0	10. 250 1, 257 1, 306 1, 361 1, 381 236 188	13 14 20 24 27 30 33 35 42 46 50 55	10. 227 1. 261 1. 332 1. 360 1. 372 1. 385 1. 154 1. 138 1. 120 1. 110 1. 102 1. 102	0 244 2808 2260 0 0 0	14 15 18 22 28 35 45 56 75 80 85	0. 197 1. 278 1. 319 1. 367 1. 420 1. 205 1. 218 1. 259 1. 293 1. 293 1. 188	0 0 256 0 0 0 0 0	13 20 28 35 40 50 70 80 88	1 0. 105 1, 362 1, 500 1, 615 1, 643 1, 323 1, 339 1, 369 1, 380 1, 321 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	

I Self-starting.

TABLE VI.—STABLE-AUTOROTATION TESTS, MONO-PLANE WING, N. A. C. A. 84

	Yaw-	00		Yaw=	5°		Yaw=1	0°		Yaw=20°		
a*	Posi- tive ro- tation pb 2V	Nega- tive ro- tation pb 2V	æ	Posi- tive ro- tation pb 2V	Nega- tive ro- tation <u>po</u>	a°	Posi- tive ro- tation po 2V	Nega- tive ro- tetion <u>p</u> o 2V	α°	Posi- tive ro- tation pb 2V	Neg- ative rota- tion pb 2V	
16	0. 324	0.322	16	(10.060 .335	a 313	14	10.073	0	12	3 0. 072	0	
18 20 22 22 25 30 32 40 60 70 80	. 360 . 380 1. 394 2. 417 1. 419 1. 405 1. 116 0 0 0	. 353 . 365 . 365 . 405 . 405 . 405 . 105 0 0	18 20 22 24 25 30 32 34 36 38 40 50 70 80	1.385; 1.387; 1.413; 1.452; 1.452; 1.450; 1.225; 1.225; 1.124; 1.185; 1.	342 .356 .366 .385 .376 .340 .000 .000 .000 .000 .000 .000 .000	16 18 20 22 24 26 30 32 32 40 45 50 70 75 80	1, 165 1, 376 1, 379 1, 450 1, 450 1, 486 1, 563 1, 570 1, 536 1, 344 1, 344 1, 263 1, 263 1, 265 1, 306 1, 315	0 .311 .335 .347 .351 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	14 16 18 20 22 24 26 30 32 32 40 42 44 45 45 60 60 60 775 80	1, 118 1, 213 1, 376 1, 414 1, 450 1, 585 1, 486 1, 480 1, 400 1, 400 1, 400 1, 400	000000000000000000000000000000000000000	

TABLE VII.—STABLE-AUTOROTATION TESTS, MONOPLANE WING, N. A. C. A. 86-M

	Yaw=0	je –		Yaw=	. Q°		Yaw≃10°			Yaw⇒20°		
a°	Posi- tive rota- tion pb	Neg- ative rota- tion pb	æ	Positive rotation po	Neg- ative rota- tion pb	a•	Positive rotation pb 2s	Neg- ative rota- tion po	α°	Posi- tive rota- tion po 20	Neg- ative rota- tion <u>pb</u>	
12 13 14 16 18 20 22 24 26 30	0.118 i.190 i.236 i.264 i.329 i.365 i.305 i.405 .434 0	0. 121 1. 193 1. 236 1. 289 1. 332 1. 359 1. 401 -418 0	13 14 15 18 20 22 24 26 28 35 40 45 50 65 60 67 77 58	10. 192 1. 234 1. 291 1. 325 1. 372 1. 405 1. 427 1. 222 1. 144 1. 123 1. 115 1. 131 1. 115 1. 185 1. 229 1. 229 1. 229 1. 227	0. 145 2111 1. 2819 1. 3819 1. 3850 0. 405 0. 00 0. 00 00 00 00 00 00 00 00 00 00 00 00 00	13 14 15 16 18 20 22 24 26 28 30 32 34 40 45 50 65 70 70 80	1 0. 171 1. 212 1. 247 1. 377 1. 373 1. 432 1. 485 1. 485 1. 234 1. 225 1. 223 1. 223 1. 225 1. 225 1. 235 1. 2	0 - 207 - 247 - 296 - 370 - 385 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	12.5 13.14 16.18 20.22 24.25 30.32 32.35 45.55 50.65 77.75 80.65 77.75 80.65 77.75 80.65 77.75	0. 094 1. 112 1. 147 1. 292 1. 338 1. 394 1. 434 1. 435 1. 557 1. 550 1. 620 1. 620 1. 294 1. 394 1. 403 1. 403 1. 403 1. 407 1. 392	000000000000000000000000000000000000000	

<sup>1</sup> Self-starting.

## TABLE VIII.—ROLLING-MOMENT TESTS, BIPLANE WING, CLARK Y

[Yaw=0°]

			•	0 ]				
	α=	-0°			α=	40°		
Positiv	e rotation	Negativ	re rotation	Positive rotation   Negative rotation			e rotation	
₽b 2V	C <sub>k</sub>	20 20	C <sub>λ</sub>	20 21√	G.	20 20	C).	
0.046 .076 .113	-0. 0186 0247 0876	0.044 .058 .094	0. 0187 . 0287 . 0358	0.100 .207 .738 .820 1.015	-0.0039 0077 +.0072 +.0037 0185	0. 153 . 248 . 705 . 815 1. 015	0.0069 +.0096 0050 0021 +.0217	
	a≃	180			α=	45°		
0.175 .293 .871 .436	+0.0080 0091 0238 0392	0. 183 -295 -375 -408	-0.0062 +.0107 .0256 .0348	0.116 .216 .945 I.017 I.074 I.140	-0.0029 0064 +.0083 +.0007 0131 0263	0. 103 . 195 . 285 . 885 . 990 1. 079	0.0043 .0071 +.0077 0065 0004 +.0154	
	a=	:30°		α=55°				
0. 347 . 530 . 626 . 710	+0.0078 0050 0163 0284	0. 432 -533 -647 -718	-0.0066 +.0037 .0208 .0315	1.027 1.094 1.204	0.0090 .0058 .0000	1. 025 1. 148	-0.0084 +.0032	
	α=	:35°			α=	·70°		
0. 170 -587 -682 -750 -817	-0.0049 +.0013 0024 0084 0154	0. 140 . 678 . 770 . 845	+0.0064 0015 +.0067 .0202	1. 198 1. 265 1. 327	0.0091 .0041 .0006	1. 144 1. 228 1. 310	-0.0075 0036 +.0004	

# TABLE IX.—ROLLING-MOMENT TESTS, BIPLANE WING, CLARK Y

[Yaw=5°]

	a=	•0°			α=	40°		
Positiv	e rotation	Negati	ve rotation	Positiv	Positive rotation Negative rotati			
pb 2V	Cì	<i>2</i> 0 2√	Сλ	20 27	C <sub>λ</sub>	$\frac{pb}{2V}$	C <sub>λ</sub>	
0.068 .085 .108	-0. 0215 0298 0367	0.082 .058 .100	0. 0130 . 0221 . 0871	0.057 .145 .238 .607	0.0058 +.0021 0003 +.0187	0.192 -274 -600 -716	0. 0164 +. 0181 0001 0010	
	α=	19°		. 828 . 934 1, 068	+.0097 0033 0341	.945	, 0078	
0. 126 . 168 . 261 . 323	0.0269 .0224 +.0072 0059	0, 218 . 280 . 871 . 433	-0.0056 +.0030 .0187	α=45°				
. 388 . 431	.3880194			0. 100 156 224	0.0038 .0023 .0005	0. 196 . 287 . 870	0.0125 +.0141 0081	
	α=	25°		. 787 . 992	.0227	.970 1.088	+.0014 .0103	
0. 169 . 246 . 371	0.0288 .0236 +.0085	0. 216 . 336 . 436	-0.0199 0078 +.0078	1.048 1.090	+. 0007 0120	1,000	, ,	
479 541	0099 0215	. 522	0235	α=50°				
	α=	30°	· · ·	0. 598	0.0212	0. 159	+0.0078	
0. 433 . 518 . 632 . 720	0.0086 +.0015 0095 0249	0.403 .531 .649 .746	-0.0077 +.0032 .0168 .0316	1.035 +.0109 .7550 1.1530030 .9200 1.2080099 1.0840 1.1900				
		850		α=55°				
0. 072 - 224 - 507 - 653 - 750 - 828 - 905	0.072 0.0065 0.178 0.0166 .224 .0072 .332 .0107 .507 .0142 .527 .0055 .653 +.0052 .643 .0053 .7500029 .885 .0229 .8280124		.0107 .0055 .0053	0. 828 . 935 1. 040 1. 100 1. 209	0.0212 .0172 .0119 .0082 .0002	1. 026 1. 143	-0.0107 +.0010	

# TABLE X.—ROLLING-MOMENT TESTS, BIPLANE WING, CLARK Y

[Yaw=10°]

	α=	6°		α=35°					
Positiv	e rotation	Negativ	ve rotation	Positiv	e rotation	Negativ	Negative rotation		
$\frac{pb}{2V}$	Сх	<u>pb</u> 2₹	Ca	$\frac{pb}{2V}$	Cà	$\frac{pb}{2V}$	Cx		
0. 037 . 060 . 097	-0. 0133 0212 0337	0.031 .068 .094	0. 0110 . 0241 . 0329	0. 511 . 688 . 742 . 838 . 896	0. 0217 . 0095 +. 0044 0092 0214	0. 138 . 224 . 532 . 744 . 850 . 899	0. 0258 . 0274 . 0136 . 0037 . 0131 . 0212		
	α=	19°			α=	40°			
0. 160 . 261 . 364 . 410	0.0249 +.0064 0166 0265	0. 227 . 315 . 438	0.0029 .0132 .0330	0. 695 . 886 . 962 1. 057	0.0266 +.0111 0039 0295	0. 085 215 300 .761 .869 .923 1. 046 1. 110	0.0200 .0247 .0260 .0035 .0044 .0038 .0168		
	<u>α=</u>		<del></del>	α=45°					
0. 233 . 375 . 485 . 531 . 571	0. 0296 +. 0101 0104 0191 0270	0. 211 . 360 . 472 . 548	-0.0082 +.0011 .0146 .0262	0.726 .817 .990 1.083 1.186	0. 0818 - 0269 +- 0103 0080 0818	0. 151 . 246 . 895 . 970 1. 078 1. 142	0. 0172 +. 0199 0027 +. 0035 . 0097		
	α=	30°		α=50°					
0. 285 . 380 . 494 . 647 . 755	0.0267 .0165 +.0086 0099 0296	0. 072 . 094 . 458 . 533 . 643 . 735	0. 0257 . 0262 . 0024 . 0071 . 0178 . 0274	0. 696 . 824 1. 065 1. 110 1. 197	0. 0265 . 0252 . 0104 +. 0063 0028	0. 201 . 892 1. 012 1. 149	+0.0121 0094 0011 +.0117		

# TABLE XI.—ROLLING-MOMENT TESTS, BIPLANE WING, CLARK Y

 $[Yaw = 20^{\circ}]$ 

	α=	•0°	·		α=	35°	
Positiv	e rotation	Negativ	re rotation	Positive rotation Negative rotation			e rotation
$\frac{pb}{2V}$	Cs.	2V	Cs.	20 20	G.	pb 2V	. G
0.047 .079 .110	-0. 0149 0239 0335	0. 650 . 090 . 119	0. 0146 . 0267 . 0355	0. 485 . 563 . 730 . 858	0. 0826 . 0287 +. 0120 0117		
ĺ	- α=15°				0342		
0.072	-0.0084 0128	0.048	0. 0235 . 0314		a=	40°	
. 252 . 317	0226 0335	.098	.0377	0, 207 . 703	0. 0272 . 0327	0. 267 1. 073	0.0872 .0122
	α=	20°		. 800 . 889	+. 0108		
0. 135 .166 .203	0. 0335 . 0278 . 0207			991 1.080	0080 0322	45*	
. 280 . 810	+.0054 0016				a-	70	
. 362 . 436	0105 0246			0. 595 . 824	0. 0870 . 0851	0. 179 . 313	0. 0267 . 0290
	α=	25°	,	1, 030 1, 115	+. 0116 0105	. 905 1. 010 1. 078	. 0029 . 0096 . 0154
0. 248 . 285 . 418 . 520	0. 0357 . 0287 +. 0087 0114				α=	.50°	
. 638	0209 0360			0.714 .946 1.170	0. 0347 . 0260	0. 210 . 950	0. 0207 . 0010
	. α=30°				+. 0115 0101	1,069	.0093
0. 287 . 330 . 462 . 573 . 638 . 703	0. 0376 .0340 .0227 +. 0083 0009 0127						

# TABLE XII.—ROLLING-MOMENT TESTS, MONO-PLANE WING, CLARK Y

 $[Yaw=0^{\circ}]$ 

			[Ya	w=0°}			
	α•	■ 0°			α	28°	
Positiv	e rotation	Negati	re rotation	Positive rotation Negative rotation			e rotation
2b 2V	G,	<i>pb</i> 2√	G <sub>A</sub>	2b 2V	C),	20 2V	a
0.078 .147 .213	-0. 0351 0628 0927	0.082 .142 .196	0. 0816 . 0567 . 0795	0. 074 . 237 . 338 . 412	-0.0041 0031 0050 0117	0.066 .227 .306 .412	0. 0023 +. 0018 0002 +. 0079
	α=	140		. 552 . 790	-, 0313 -, 0934	. 570 . 703	.0315
0.080 .085 .208	-0.0096 0087 +.0117	0.063 .101 .231 .306	0.0107 +.0134 0059 +.0117		α=	·30°	
. 250 . 255 . 306 . 309 . 477	+.0011 0011 0040 0152 0641	. 477	.0365	0. 104 . 263 . 302 . 362 . 411	-0.0059 0062 0079 0096 0127	0. 105 . 227 . 315 . 362 . 399	0.0050 .0047 .0090 .0090 .0085
	α=	20°		. 451 . 574 . 551	0156 0294 0468	. 556 . 688	. 0242 . 0503
0. 129 . 170 . 246 . 339 . 494	0.0308 .0279 +.0163 0031 0423	0. 136		. 002		40*	
632	-: 0791	. 560	. 0578	0.095	0.0074	0. 078	0.0043
	α=	25°			0149 0268 0402	.170 .285	.0089
0. 048 . 265 . 393 . 582	-0.0010 +.0065 0096 0457	0.044 .278 .371 .665	-0.0011 0085 +.0037 .0648	. 680	-, 0402	.449 .720	. 0265 . 0415

# TABLE XIII.—ROLLING-MOMENT TESTS, MONO-PLANE WING, CLARK Y

### [Yaw=5°]

	α <b>=</b>	·0°			æ	33°		
Positiv	e rotation	Negativ	re rotation	Positiv	rotation	Negativ	e rotation	
$\frac{pb}{2V}$	G.	<i>pb</i> 2 <i>V</i>	C <sub>λ</sub>	20 2√	G	<i>p</i> b 2∇	·Ca	
0.082 .153 .203	-0.0371 0665 0675	0.078 .138 .185	0. 0302 . 0533 . 0785	0.075 .110 .190 .345	0.0080 +.0081 0026 0086	0.089 .222 .360 .496	0. 0150 . 0208 . 0228 . 0265	
	α=	13°		.473 .726	0109 0418	. 625 . 749	. 0375 . 0542	
0.073 -137	-0.0099 0143	0.055	0. 0146 . 0348	<i>:</i>	α=	50°		
220 269 276 379 498 591	003 0008 0099 0122 0410 0796 1137	0099 .257 .0085 0122 .278 .0124 0410 .280 .0180 0796 .310 .0192		0.095 .208 .315 .436 .550 .638	+0.0004 0048 0117 0203 0286 0349	0. 182 . 224 . 328 . 468 . 676 . 835	0.0127 .0172 .0201 .0323 .0440 .0540	
		.466	0628	α≖65°				
	α=	20°		0.125 .231	+0.0002 0017	0.188 .274	0.0073 .0085	
0. 128 . 218 . 284 . 332	0.0418 .0279 .0128 -10025	0.178 .255 .849 .610	-0.0194 0103 +.0085	.819 .458 .585 .695	0054 0118 0179 0232	.408 .500 .692	.0123 .0147 .0237	
.444 .617	- 0274 - 0780	.010	.0/11	α=		α=80°		
	α=	27°		0. 139 261 407 550	+0.0002 0002 0021 0035	0.166 .291 .485 .623	0.0012 .0013 .0016 .0021	
0.067 246	0.0066 0104	0.097 .317	0.0135 .0061	.722	- 0039	.865	.0015	
.371 .513 .665	+.0006 0229 0561	. 432 . 660	.0192 .0564		α=	85°		
.000	0001			0. 132 . 280 . 447 . 583 . 790	-0.0003 0006 0011 0015 0017	0. 159 . 328 . 589 . 780 . 955	-0.0002 0002 0005 0007 0014	

# TABLE XIV.—ROLLING-MOMENT TESTS, MONO-PLANE WING, CLARK Y

### [Yaw=10°]

	a=	•0•			a=	50°		
Positiv	Positive rotation   Negative rotation				Positive rotation   Negative rotation			
<u>⊅</u> b 2√	G <sub>A</sub>	<i>2</i> 0 2 <i>V</i>	C.	20 20	Cs.	<u>p</u> ò 2√	C).	
0.060 .110 .147	-0.0279 0470 0625	0.103 .113 .176	0. 0405 . 0430 . 0682	0.062 .134 .237 .393	0.0062 +.0027 0021 0130	0.140 .272 .574 .662	0.0179 .0237 .0415 .0465	
	a=	15°		.516 .750	0214 0322			
0.163 .235	0.0271 +-0117	0.047	0.0321 .0114		α=65°			
. 285 . 460 . 528	- 0010 - 0521 - 0780	.382 .480	. 0253 . 0556	0.093 .222 .410	0.0042 +.0011 0076	0. 147 . 371 . 621	0.0098 .0119 .0202	
	a=	220		. 595 . 761 · 1. 000	0173 0230 0277	.811 .027		
0.201 .311 .455	0.0324 +-0137 0204	0. 220 . 332 . 436	0.0005 .0063 .0260		a=	α=80°		
. 580	0829	.563	. 0545	0.146 .302	+0.0010 0002	0.148	0.0017 .0014	
	α=-	·28°	<u> </u>	.855  003	0035 0036	.466 .630 .863	.0012 .0013 .0021	
0.176 .222 .281	0.0176 .0159 .0131	0.108 .210 .373	0.0232 .0210 .0191	.992	0035	<u> </u>		
.410 .628 .733	+. 0023 0393 0692	. 520 . 690	.0250 .0607		α=85°			
. 100		<u> </u>	<u> </u>	0.172 .319	-0.0004 0005	0. 233 . 458	+0.0002 0002	
	α=	·85°		. 565 . 696 . 830	0004 0013 0011	. 680 . 879	+.0003 0006	
0.052 .084 .160 .257 .490 .645 .835	0.0121 .0097 +.0082 0084 0055 0135 0544	0.108 -214 -434 -710	0.0220 .0281 .0346 .0482					

# TABLE XV.—ROLLING-MOMENT TESTS, MONO-PLANE WING, CLARK Y

[Yaw=20°]

	. a=	=0°		-	α=	450	
Positiv	re rotation	Negative rotation		Positive rotation		Negativ	e rotation
20 20	C),	$\frac{pb}{2V}$	C <sub>λ</sub>	ρδ 2V	c,	2V 2V	C <sub>3</sub> .
0. 111 . 169 . 255	-0.0447 0650 0966	0.101 .168 .210	0. 0802 . 0525 . 0701	0, 107 235 309 . 525	0. 0149 +. 0062 0028 0106	0. 158 . 354 . 499 . 660	0. 0318 . 0392 . 0430 . 0551
	α=	15°		.805	0089	<u> </u>	}
0. 108	0.0420	0, 055	0.0514	::	· &=	60°	
. 224 . 287 . 401 . 516	+. 0133 0031 0363 0709	. 147 . 358 . 467 . 540	. 0575 . 0872 . 0493 . 0684	0.122 212 815 405	0.0098 .0060 +.0018 0034	0. 128 . 246 . 505 . 718	0. 0185 . 0218 . 0205 . 0321
	α=	20°		896	0174 0318		
0.108 .233	0.0615 .0382	0, 240 . 341	0. 0254 . 0264		a=	75°	
. 317 . 432 . 607	+. 0125 0174 0684	.548 .678 .751	. 0510 . 0827 . 1040	0.145 .978 .418	0.0049 +.0032 0013	0.135 .274 .612	0. 0077 . 0078 . 0065
	α=	28°		. 522 . 808	0029 0058	.748	0086
0.167 .279	0. 0487 . 0867	0, 135 . 452	0.0443 .0355	-	· α=	85°	· ·
. 434 . 609 . 747	+. 0173 0294 0681	.617	.0641	0. 187 . 817 . 585	0.0013 .0009 .0004	0. 183 . 444 . 600	0.0015 .0011 .0009
	α=	35°	_	1.010	.0000	.740 .905	+. 0005 0008
0. 087 . 215 . 465 . 596 . 715	0. 0228 .0132 .0168 +. 0030 0179	0. 183 . 264 . 534 . 700	0. 0382 . 0440 . 0514 . 0600				

# TABLE XVI.—ROLLING-MOMENT TESTS, MONO-PLANE WING, N. A. C. A. 84

[Yaw=0°]

1, , ,									
α=	-6°			a=	220				
Positive rotation	Negati	ve rotation	Positiv	e rotation	Negativ	e rotation			
$\frac{pb}{2V}$ $C_{\lambda}$	<i>pb</i> 2 <i>V</i>	Сх	<i>p</i> ₀ 2 <i>V</i>	C).	20 2V	C)			
0.063 -0.0225 .1090411 .1530590	0.056 .091 .120	0. 0288 . 0385 . 0498	0. 187 . 215 . 245 . 263	0. 0493 . 0426 . 0371 . 0326	0.112 .182 .219 .258	-0.0460 0487 0362 0333			
· an	-0°		.841 .417 .458	+. 0142 0014 0117	. 329 . 408 . 478	0149 +.0041 .0218			
0.037 -0.0016 .0780312 .1430596	0.039 .067 .088	0. 0206 . 0324 . 0407		α=:	≱4°				
α:	=6°	<u> </u>	0. 184 . 255 . 366 . 423	.0321 .24500 .0148 .3410					
0. 070 -0. 0277 .104 0404 .128 0515	0.071 .111	0. 0330 . 0498	. 806	—. 0160 α=1	. 507	0208			
α=	-12°		0.001	0, 0134	<u></u>	0.0100			
0.067 -0.0204 .1270417 .1900545	0.071 .119 .149	0.0259 .0392 .0471	0. 351 . 423 . 470 . 555	+. 0009 0073 0260	0. 351 . 423 . 478 . 568	-0.0128 0008 +.0107 +.0304			
		.0471		α=	10°				
<u> </u>	-16°	·	0.404 ,482	+0.0017 0032	0.404	-0.0010 +.0049			
0.061 -0.0113 .1140180 .269 +.0139	0.086 .194 .201 .351	0.0155 +.0120 0134	. 554	0161	. 547	. 0180			
.878 — .0098 .392 — .0148	.359	+.0080 +.0108		α=t	350				
α=	-18°		0, 164 , 269 , 407	-0.0037 0093 0122	0. 164 . 255 . 394	0.0042 .0095 .0118			
0. 204 0. 0391 . 283 . 0327 . 319 + . 0124 . 392 0087	0. 213 . 238 . 319 . 407	-0.0851 0812 0113 +.0145	.519	0146	. 513	, 0146			
α=	-20°								
0. 172 0. 0417 .223 .0386 .247 .0325 .341 +.0120 .4230093	0. 177 . 227 . 263 . 335 . 407	-0.0426 0354 0296 0117 +.0073		·					

## TABLE XVII.—ROLLING-MOMENT TESTS, MONO-PLANE WING, N. A. C. A. 84

### [Yaw=10°]

	a=	-6°			α=	:22°		
Positiv	re rotation	Negative rotation		Positive rotation		Negativ	e rotation	
<i>pb</i> 2 <i>V</i>	C <sub>k</sub>	<i>2</i> 0 2√	G <sub>k</sub>	<i>p</i> ∂ 2V	Cs.	<u>pb</u> 2√	C),	
0.046 .061 .085 .112	-0. 0164 0222 0259 0435	0.057 .085 .118	0. 0248 . 0357 . 0498	0. 099 . 239 . 290 . 878 . 425	0.0676 0448 0351 0129 +.0019	0.272 .351 .419 .468 .527	-0.0109 +.0002 .0136 .0249 .0382	
	α=	-0°		. 507	0222		_	
0,054	-0.0203 0306	0. 051 . 085	0.0273 .0415		α=	·24°		
.138	0538	.120	.0545	0. 132 . 263	0.0567 .0423	0.353 .502	0.0005 .0262	
	α=	=6°		.316 .400 .505	0310 +. 0129 0127	.560	.0411	
0.064 .093 .138	-0.0202 0316 0492	0.060 .099 .128	0. 0322 . 0468 . 0587	550	02 <del>4</del> 3	:26°		
!——— !	α=	-12°		0. 168	0.0438	0.327	0.0008	
0.069 .095 .142 .190	-0.0088 0161 0293 0441	0.071 .115 .144	0. 0368 . 0495 . 0585	.243 .300 .417 .576	0404 0827 + 0139 - 0233	.429 .502 .590	.0120 .0244 .0408	
	<u>.                                    </u>	160		α=30°				
0.068 .189 .270 .333 .366 .405	+0.0074 0043 +.0142 0028 0121 0225	0.117 .843 .421 .508	0. 0443 . 0111 . 0279 . 0588	0.046 .116 .447 .562 .615	0.0304 .0268 +.0148 0050 0149	0.115 .337 .425 .543 .630	0.0284 .0126 .0179 .0294 .0418	
	l	<u> </u>	<u></u>		α=	35°		
	α=	18*	<u> </u>	0. 219	0.0108	0.084	0.0269	
0. 170 . 247 . 329 . 878 . 400 . 492	0. 0505 . 0345 . 0125 0015 0100 0319	0.335 .462 .527	0.0036 .0328 .0527	. 535 . 641 . 690	+. 0027 0044 0116	. 147 . 221 . 298 . 421 . 540 . 654	.0277 .0297 .0303 .0301 .0337 .0411	
α=20°								
0. 136 - 186 - 235 - 278 - 353 - 447 - 490	0.0625 .0527 .0432 .0327 +.0124 0124 0237	0.349 .468 .540	0.0023 .0281 .0472					

## TABLE XVIII.—ROLLING-MOMENT TESTS, MONO-PLANE WING, N. A. C. A. 86-M

### [Yaw=0°]

	α=	•0°			α=	35°	-
Positiv	e rotation	Negativ	ve rotation	Positiv	e rotation	Negativ	s rotation
20 2√	C).	<u>Pò</u> 2 <i>V</i>	G.	<u>pŏ</u> 2 <i>V</i>	C <sub>3</sub> .	<i>pb</i> 21∕	C),
0.069 .103 .129 .165	-0.0319 0465 0670 0732	0.069 .109 .160	0. 0348 - 0493 - 0708	0. 102 -236 -383 -547 -679	-0.0052 0127 0242 0274 0299	0. 139 .247 .388 .541 .730	0.0105 .0154 .0225 .0299 .0413
	a=	·10°		.739 .812	- 0379 - 0581	.788	.0518
0.084	-0.0214 0282	0.069	0.0208 .0212	1	α=	40°	
.272 .327 .378	0401 0846 0680	.156 .240 .321 .361	. 0221 . 0830 . 0506 . 0589	0. 158 -278 -367 -577 -610	-0.0094 0151 0222 0376 0390	0.139 .280 .340 .429 .498	0. 0103 . 0166 . 0220 . 0284 . 0334
	α <del>-</del>	15°		.748 .832	- 0435 - 0497	. 552 . 719 . 792	.0370 .0426 .0475
0.201 .287 .229	+0.0131 0044 0147	0. 200 . 287 . 358 . 438	-0.0183 +.0055 .0255	α=50°			·
. 530 . 530	0303 0746	.487	.0655	0.036	-0.0044 0103	0.138	0.0060 .0122
	a=	20°		.311 .472 .677	- 0127 - 0246 - 0385	.381 .443 .589	.0151 .0242 .0303
0.307 .876 .418	+0.0152 0031 0113	0.801 .876 .445	-0.0141 +.0036 .0219	.757	<b>—. 0453</b>	. 695 . 795	. 0409 . 0458
.487 .579 .601	0813 0601 0685	. 506 . 588	.0398 .0628		α-	65°	
	a=	·25°	l	0.196 .314 .443 .541	-0.0031 0057 0123 0168	0.181 .301 .450 .570	0.0047 .0065 .0141 .0189
0.053 .874	-0.0025 +.0158	0.115	+0.0046	.661 .760	0217 0258	.704	.0241
.445 .516 .581 .625	+.0013 0158 0815 0467	.405 .478 .554 .623	+.0002 .0132 .0287 .0464		α=	80°	
.677	. —. 0620			0. 294 . 432	-0.0001 0016	0.311 .416	0.0014 .0023
ļ	α=	*30°	<u>.                                    </u>	. 543 . 605 . 695	0027 0032 0038	. 515 . 672	.0033 .0046
0. 097 . 221 . 369 . 525 . 637 . 695 . 752	-0.0041 0105 0146 0213 0415 0512 0017	0. 132 . 233 . 521 . 625 . 699	0.0060 .0128 .0206 .0349 .0504				

# TABLE XIX.—ROLLING-MOMENT TESTS, MONO-PLANE WING, N. A. C. A. 86-M

#### [Yaw=5°]

#### α=35° α=0° Positive rotation | Negative rotation Positive rotation Negative rotation 2V $C_{\lambda}$ -0.0055 -.0170 -.0196 -.0274 -.0421 -0.0288 -.0442 -.0561 -.0706 0.0249 .0858 .0506 .0690 0. 225 . 367 . 521 . 648 . 750 0. 121 . 263 . 381 . 552 . 699 0.0176 .0247 .0308 .0377 0.049 .099 .128 .168 0.048 .074 .110 .159 . 0466 α=10° α=40° -0. 0198 -. 0351 -. 0548 -. 0751 0.124 .258 .278 .847 .894 0. 0299 . 0390 . 0427 . 0580 . 0708 0, 152 . 256 . 332 . 401 -0.0056 -.0141 -.0237 -.0301 -.0357 0. 185 . 240 . 354 . 454 . 570 . 681 0. 0175 . 0232 . 0281 . 0366 . 0445 . 0482 0. 225 . 829 . 465 . 568 . 786 α=15° $\alpha = 50^{\circ}$ +0.0143 -.0009 -.0167 -.0306 -.0464 -.0586 -0.0185 +.0045 .0215 .0341 .0481 0, 192 .267 .827 .872 .430 .468 0. 167 . 272 . 847 . 885 . 432 . 494 -0.0047 -.0111 -.0193 -.0247 -.0326 -.0408 0. 167 . 247 . 363 . 501 . 681 . 793 0. 0150 . 0189 . 0227 . 0385 . 0452 . 0513 0. 296 . 352 . 463 . 543 . 670 . 768 α=20° α=65° 0. 197 . 312 . 392 . 432 . 568 0.0401 +.0153 -.0060 -.0168 -.0597 -0.0251 -.0148 +.0040 .0168 .0500 .0687 0. 208 . 285 . 372 . 418 . 539 . 597 -0.0029 -.0089 -.0146 -.0196 -.0235 0, 814 . 448 . 548 . 668 . 760 0.0091 .0118 .0158 .0220 .0255 .0292 0. 243 . 874 . 459 . 597 . 697 . 797 α=25° α=80° 0.325 .403 .560 .632 0. 0283 +. 0181 -. 0258 -. 0498 0. 316 . 396 . 521 . 686 -0.0049 +.0019 .0249 .0531 0. 418 . 650 . 804 -0.0014 -.0029 -.0027 0. 412 . 547 . 708 . 795 0.0040 .0058 .0073 .0075 α=30° +0.0084 -.0034 -.0060 -.0096 -.0283 -.0391 -.0507 0.042 .225 .412 .483 .574 .650 0. 083 . 186 . 307 . 450 . 561 . 670 0. 0158 . 0207 . 0231 . 0241 . 0815 . 0491

### TABLE XX.—ROLLING-MOMENT TESTS, MONO-PLANE WING, N. A. C. A. 86-M

[Yaw=10°]

			<del></del>					
	α=	•0°			α=	·35°		
Positiv	e rotation	Negative rotation		Positive rotation		Negativ	e rotation	
$rac{pb}{2V}$	C <sub>2</sub>	<u>pb</u> 2V	C),	$\frac{pb}{2V}$	C),	<i>pb</i> <b>2</b> <i>V</i>	C).	
0.049 .093 .139 .178	-0. 0211 0391 0584 0711	0.046 .067 .102 .155	0. 02±0 . 0326 . 0450 . 0659	0.098 .260 .347 .463 .561	-0.0110 0024 0086 0086 0125	0. 104 . 222 . 314 . 443 . 565 . 683	0. 0254 . 0325 . 0354 . 0417 . 0455 . 0521	
	α=	10°		.072	0233		.0521	
0.056	-0.0158	0.065	-0.0166		α=	40°		
.146 .201 .261 .307 .354	0201 0278 0392 0508 0645	. 073 . 113 . 265 . 354	+. 0244 . 0340 . 0485 . 0647	0. 063 234 . 831 . 436 . 583 . 688	+0.0105 0007 0081 0156 0219 0261	0.091 .227 .361 .458 .581 .668	0. 0221 . 0304 . 0341 . 0432 . 0508 . 0587	
	α=	15°		780	0315	5 .008 .0087		
0.077 .175	0.0252 +.0149	0. 115 . 225	-0.0087 +.0028	α=50°				
. 278 . 827 . 886 . 425 . 461	0064 0208 0371 0516 0654	. 287 . 361 . 416 . 468	. 0128 . 0283 . 0420 . 0569	.683	+0.0088 0015 0182 0219 0295	0. 134 . 240 . 325 . 441 . 588	0. 0198 . 0240 . 0268 . 0817 . 0438	
	α=	20°		. 779	<b> 0375</b>	. 692 . 788	. 0502 . 0559	
0. 197 . 812	0.0401 +.0120	0.202	-0.0230 0144		α=	65°		
.452 .501 .552	0239 0369 0578	. 258 . 334 . 458 . 518 . 565	+. 0005 . 0293 . 0445 . 0606	0. 329 . 452 . 583 . 690 . 799	-0.0017 0075 0181 0171 0200	0. 179 . 296 . 458 . 597 . 721	0. 0120 .0124 .0168 .0219 .0275	
	α=	25°			α=	contr		
0.158 .392 .458 .577 .625	0. 0131 . 0153 . 0005 . 0938 . 0520	0. 369 . 465 . 577 . 652	0.0044 .0170 .0401 .0615	0.816 .458 .574	+0.0004 0017 0027	0. 234 . 365 . 450	0. 0030 . 0030 . 0037	
	α=	30°		. 672 . 806	0036 0029	. 553 . 699 . 852	.0044 .0054 .0054	
0. 122 . 443 . 512 . 612 . 712	0.0115 +.0017 0071 0270 0498	0.108 .243 .327 .470 .599 .688	0. 0269 . 0325 . 0330 . 0318 . 0422 . 0565					

# TABLE XXI.—ROLLING-MOMENT TESTS, MONO-PLANE WING, N. A. C. A. 88-M

[Yaw=20°]

	α-	=8°			a=	35°		
Positiv	e rotation	Negative rotation		Positiv	e rotation	Negative rotation		
<u>på</u> 2√	· Ca	$\frac{pb}{2V}$	C <sub>3</sub>	<i>pb</i> 2 <i>V</i>	C),	20 2V	C).	
0. 054 . 069 . 131 . 174 . 206	-0.0181 0297 0452 0596 0715	0.061 .104 .145 .199	0.0278 .0426 .0683 .0737	0. 225 . 532 . 681 . 748 . 804	0. 0155 +- 0057 0105 0242 0378	0.137 .316 .515 .712	0.0430 .0597 .0541 .0627	
	a=	10°	•		α=	40°		
0.071 .159 .225 .274 .343	-0.0150 0251 0380 0490 0656	0.065 .101 .151 .274	0.0240 .0341 .0485 .0680	0. 195 . 396 . 461 . 581 . 688 . 799 . 855	0. 0130 +. 0007 0020 0064 0088 0195 0329	0. 133 . 238 . 378 . 556 . 688	0. 0383 - 0423 - 0488 - 0550 - 0623	
	a=	15°		. 800	α=	EUG .	-	
0. 104 . 214 . 307 . 365 . 410 . 445	+0.0118 0025 0217 0363 0491 0618	0. 142 . 238 . 303 . 381 . 461	0. 0238 . 0285 . 0349 . 0449 . 0550	0. 168 . 398 . 465 . 595 . 699	0. 0123 . 0000 0043 0136 0203	0. 186 .303 .476 .614 .708	0. 0322 . 0388 . 0372 . 0491 . 0540	
	α=	20°		.8210264 α=65°				
0. 197 . 287 . 327 . 458 . 528	0.0257 .0122 +.0031 0329 0572	0. 222 .314 .372 .447 .568	0.0025 .0129 .0207 .0290 .0568	0.095 .414 .574 .870	0. 0117 +. 0012 0058 0096	0. 178 . 305 . 472 . 596	0.0186 .0192 .0192 .0238	
	α=	25°		.792	—. 0136	.681 .776	.0277	
0. 146 - 285	0. 0449 . 0367	0.127 .214	0.0442 -0455		- α=	30°		
.403 .477 .521 .601	+.0173 0044 0217 0518	.372 .503 .619 .688	.0264 0.0328 .0521 .0680	0.410 .584 .699 .790	+0.0009 0001 0006 0009	0. 182 .327 .461 .587	0.0055 .0050 .0054 .0057	
	α=	30°				.705 .830	.0070 .0071	
0.085 .481 .550 .699 .767	0. 0308 . 0160 +. 0027 0330 0622	0.094 .222 .338 .572 .681	0. 0435 . 0507 . 0516 . 0478 . 0583					

# TABLE XXII.—TEST ANGLES OF ATTACK AND YAW IN N. A. C. A. STANDARD EQUIVALENTS

Angle of	Angle of	Angle of	Angle of	Angle of	Angle of	Angle of	Angle of
sitack	attack	yaw	yew	attack	attack	yaw	yaw
(test)	(std.)	(test)	(std.)	(test)	(std.)	(test)	(std.)
0 15 30 45 60 75	0 0 14 55 29 45 44 38 59 40 74 50 90 0	10 10 10 10 10 10 10	10 0 9 40 8 40 7 0 4 50 2 24 0 0	0 15 30 45 60 75	0 0 0 14 25 29 10 43 45 59 5 74 45 90 0	20 20 20 20 20 20 20 20	20 0 19 15 17 20 14 5 10 10 5 35 0 0